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**MATH 425 Homework 1. Due Friday, Sep. 19, BEFORE  
THE CLASS STARTS**

**Problem 1.** How many different letter arrangements can be made from the letters PROBABILITY.

**Problem 2.** There are 130 students at a school and three dormitories A, B, and C with capacities 30, 35, and 65 respectively.

- (a) How many ways are there to fill up the dormitories?
- (b) Suppose that of the 130 students, 60 are men and 70 are women and that A is an all men's dorm, B is an all women's dorm and C is co-ed. How many ways are there to fill up the dormitories?

**Problem 3.** In how many ways can ten people be seated in a row if:

- (a) there are no restrictions on the seating arrangement?
- (b) persons A and B must sit next to each other?
- (c) there are 5 men and they must sit next to each other?
- (d) there are 5 men and 5 women, and no 2 men or 2 women can sit next to each other?

**Problem 4.**

- (a) How many 4 digit integers greater than or equal to 6000 (hence 6000, 6001, ..., 9999) have both of the following properties?
  - The digits are distinct.
  - The digits 2 and 7 do not occur.
- (b) How many 4 digit integers greater than or equal to 5400 (hence 5400, 5401, ..., 9999) have the same properties?

**Problem 5.** Suppose there are 8 women and 6 men. A committee consisting of 3 men and 3 women is to be formed. How many different committees are possible under each of the following conditions.

- (a) 2 of the men (Mr. X and Mr. Y) refuse to serve together.
- (b) 1 man (Mr. X) and 1 woman (Ms. A) refuse to serve together.

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**Problem 6.** In the expansion of  $(a + 3b)^{12}$ , what is the coefficient of  $a^4b^8$ ?

**Problem 7.** There are 14 people to attend a dinner party and sit at a round table.

(a) How many ways can these 14 people be arranged at the table? (Two seating arrangements are equivalent if one is a rotation of the other.)

(b) Suppose there are 7 men and 7 women. How many seating arrangements are there if no two men are to sit together.

**Problem 8** How many integer solutions of:

$$x_1 + x_2 + x_3 + x_4 = 32$$

satisfy,  $x_1 \geq 1$ ,  $x_2 \geq -4$ ,  $x_3 \geq 0$ , and  $x_4 \geq 3$ ? (Hint: Set  $y_1 = x_1 - 1$ ,  $y_2 = x_2 + 4$ ,  $\dots$ )