

Log in to your umich account, open Maple (from the dock or applications folder), then click on **File**, then select **New**, then click on **Worksheet Mode**. Type each command below and hit return to get the result. You may use the arrow keys or mouse to maneuver.

**arithmetic**

- > 2+2
- > 2^6
- > sqrt(64)
- > a:=3            *Be sure to include the colon before the equal sign.*
- > a^2
- > Pi
- > evalf(Pi)      *evalf = evaluate*

You can put several commands on a single line.

- > sin(Pi); cos(Pi); tan(Pi)
- > erf(0); erf(1); evalf(erf(1))       $\text{erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$  : *error function (see hw3)*
- > abs(-1)
- > I; I^2             $I = \sqrt{-1}$ , an *imaginary number*, written “i” in math books
- > exp(1); evalf(exp(1))
- > exp(Pi\*I)            *that’s right,  $e^{\pi i} = -1$ ; you’ll learn why in December*

**limits**

- > with(student)            *This loads the student commands.*
- > Limit(1/x,x=infinity)      *Use the right arrow key after 1/x.*
- > value(%)            *“%” refers to the expression on the previous line.*
- > limit(1/x,x=infinity)      *Limit displays the limit, limit evaluates it.*
- > limit(1/x,x=0)
- > limit(1/x,x=0,left); limit(1/x,x=0,right)      *This gives the one-sided limits.*
- > limit(x\*exp(-x),x=infinity)      *Maple knows l’Hopital’s rule.*

**plotting**

At the top of the screen, click **Maple 2015**, then **Preferences**, then **Display**, then in the **Plot display** menu, change **Inline** to **Window**, and click **Apply to Session**. This opens each plot in a separate window.

- > plot(1/x,x=0..5,y=0..5)            *After viewing, close the window to avoid clutter.*
- > plot([1/x,1/x^2],x=0..5,y=0..5)      *Which curve is 1/x? ... 1/x^2?*
- > plot(tan(x),x=-2\*Pi..2\*Pi,y=-4..4)      *tan(x) has vertical asymptotes at  $x = \pm\pi/2, \dots$*
- > limit(tan(x),x=Pi/2)
- > limit(tan(x),x=Pi/2,left); limit(tan(x),x=Pi/2,right)
- > plot(arctan(x), x=-2\*Pi..2\*Pi,y=-4..4)      *arctan(x) has horizontal asymptotes as  $x \rightarrow \pm\infty$*
- > limit(arctan(x),x=infinity)
- > plot([exp(-x),exp(-x^2)],x=0..3,y=0..1)      *Which curve is  $e^{-x}$ ? ...  $e^{-x^2}$ ?*

The next plot is an example of a parametric curve using polar coordinates.

- > plot([sin(4\*t),t,t=0..2\*Pi],coords=polar)      *Try changing 4 to 7 (for example).*

Maple has a help facility, e.g. the next command opens a window with help about plotting.

- > ?plot

## Riemann sums

> rightbox(x^2,x=0..1,2) *This plots the right-hand Riemann sum for  $\int_0^1 x^2 dx$  with  $n = 2$ .*  
> rightsum(x^2,x=0..1,2); evalf(%) *This evaluates the Riemann sum.  $\Delta x = ?$ ,  $x_i = ?$*

Repeat for  $n = 4, 8, 16$  (use the arrow keys or mouse to maneuver). Do the results converge to the correct value as  $n$  increases? The commands for the left-hand and midpoint Riemann sums are **leftbox**, **leftsum**, **middlebox**, **middlesum**. Repeat the previous commands, substituting *left* and *middle* in place of *right*. For a given value of  $n$ , which sum is the most accurate?

## antiderivatives

> Int(x^n,x); value(%)  
> int(x^n,x) *Int displays the integral, int evaluates it.*  
> int(ln(x),x); diff(%,x)  
> int(1/(x^2+1),x); diff(%,x)  
> int(1/sqrt(x^2+1),x); diff(%,x) *We'll discuss  $\sinh(x)$  later in the semester.*  
> int(exp(-x^2),x); diff(%,x) *recall:  $\operatorname{erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$*   
> f:=x^3/sqrt(1-x^8); int(f,x) *We can also substitute to find the antiderivative, as follows.*  
> a:=Int(f,x)  
> b:=changevar(x^4=u,a)  *$u = x^4$ ,  $du = 4x^3 dx$*   
> c:=value(b)  
> d:=subs(u=x^4,c); diff(d,x) *This returns to the original variable and checks the answer.*

## definite integrals

> Int(x,x=a..b); value(%) *Oops! - we need to clear variables a and b.*  
> a:='a'; b:='b'; Int(x,x=a..b); value(%) *ok*  
> Int(sqrt(1-x^2),x=-1..1); value(%) *This gives the area of a semi-circle with radius 1.*  
> Int(1/x^2,x=1..infinity); value(%)  
> Int(1/x^2,x=-1..1); value(%)  
> Int(1/x,x=1..infinity); value(%)  
> Int(exp(-x),x=0..infinity); value(%)  
> Int(x\*exp(-x),x=0..infinity); value(%) *Maple knows integration by parts.*  
> Int(exp(-x^2),x=0..infinity); value(%) *This requires multivariable calculus (Math 255).*

**surfaces in 3D** (try these for fun, use the mouse to rotate the surface)

> with(plots)  
> sphereplot(1,theta=0..2\*Pi,phi=0..Pi) *sphere*  
> plot3d(x^2-y^2,x=-1..1,y=-1..1) *saddle*  
> plot3d([r\*cos(theta),r\*sin(theta),r],r=0..1,theta=0..2\*Pi) *cone*  
> plot3d([(1+.2\*cos(a))\*cos(b),.2\*sin(a),(1+.2\*cos(a))\*sin(b)],a=0..2\*Pi,b=0..2\*Pi) *torus*

**Homework Assignment** (hand in with hw4 on Tuesday Oct 3)

In class and on hw we computed Riemann sums for the integral  $I = \int_0^1 f(x) dx$  with  $f(x) = e^x, e^{-x}$ , and found that if  $\Delta x$  decreases by a factor of  $1/2$ , then the error in the right-hand Riemann sum  $R_n$  decreases by about  $1/2$  and the error in the midpoint Riemann sum  $M_n$  decreases by about  $1/4$ . Is the same true for  $f(x) = \sqrt{x}$ ? To answer this question, construct a table with the following data (you may use Maple or a calculator). column 1:  $n$  (take  $n = 2, 4, 8, 16$ ), column 2:  $\Delta x$ , column 3:  $R_n$ , column 4:  $|I - R_n|$ , column 5:  $M_n$ , column 6:  $|I - M_n|$ . For a given value of  $n$ , which method gives a more accurate answer? How do the results for  $\sqrt{x}$  compare with the results for  $e^x, e^{-x}$ ? What is similar? ... different? Explain your observations.