

Some Possibly Useful Formulae.

$$\vec{\nabla} = \left\langle \frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z} \right\rangle, \quad \operatorname{div} \vec{F} := \nabla \cdot \vec{F}, \quad \operatorname{curl} \vec{F} := \nabla \times \vec{F}.$$

$$dA(x, y) = dx dy = dy dx. \quad dA(r, \theta) = r dr d\theta = r d\theta dr.$$

$$dV(x, y, z) = dx dy dz = dx dz dy = \dots,$$

$$dV(r, \theta, z) = r dr d\theta dz = r d\theta dr dz = \dots,$$

$$dV(\rho, \theta, \phi) = \rho^2 \sin(\phi) d\rho d\theta d\phi = \rho^2 \sin(\phi) d\theta d\phi d\rho = \dots.$$

$$dS = \sqrt{1 + z_x^2 + z_y^2} dA(x, y) = \|\vec{r}_u(u, v) \times \vec{r}_v(u, v)\| dA(u, v).$$

$$\int_C \vec{\nabla} \phi \cdot d\vec{r} = \phi(\vec{r}(b)) - \phi(\vec{r}(a)).$$

$$\oint_C \vec{F} \cdot d\vec{r} = \iint_D (Q_x - P_y) dA.$$

$$\int \sin^2(u) du = \frac{1}{2}u - \frac{1}{2} \sin(u) \cos(u) + C$$

$$\int \sin^4(u) du = \frac{3}{8}u - \sin(u) \left[\frac{3}{8} \cos(u) + \frac{1}{4} \sin^2(u) \cos(u) \right] + C$$

$$\int \sin^6(u) du = \frac{5}{16}u - \sin(u) \left[\frac{5}{16} \cos(u) + \frac{5}{24} \sin^2(u) \cos(u) + \frac{1}{6} \sin^4(u) \cos(u) \right] + C$$

$$\int \sin^8(u) du = \frac{35}{128}u - \sin(u) \left[\frac{35}{128} \cos(u) + \frac{35}{192} \sin^2(u) \cos(u) + \frac{7}{48} \sin^4(u) \cos(u) + \frac{1}{8} \sin^6(u) \cos(u) \right] + C.$$